A Novel Micro Flow-Focusing Device for the Control of Droplet Contents

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Abstract- Micro flow-focusing devices (mFFDs) have been used extensively to produce emulsions and for the on-line encapsulation of biologic objects, such as bacteria and cells. More recently, new designs of this type of instrument have been imagined, for example to produce multi-layered capsules. In this work, we present a novel design of mFFD that comprises “moustaches”, i.e. escape microchannels, just upstream of the orifice. In the context of encapsulation, such a design authorizes the control of the number of biologic objects imprisoned in a single capsule, and avoids the emission of empty capsules. We have denoted this new type of FFD by the abbreviation EFFD, for “Escape FFD”. We first present the concept of the system, then we derive the pressure conditions for the proper functioning of the device, and finally we present an experimental realization.

Keywords- Flow-Focusing Device; Encapsulation; Meniscus Stability; Interface Breakup; Escape Channels

1. INTRODUCTION

In the modern approach of microfluidics, the use of individual droplets has been constantly increasing. Droplet and digital microfluidics are now essential tools in many domains such as biotechnology and material sciences [1, 2]. Manipulation of single droplets has seen recently many developments [3, 4]. In this work we present a new concept of micro flow-focusing device for a better control of encapsulation process.

Micro flow-focusing devices (mFFDs) have been used extensively to produce emulsions, to perform in-drop chemical reactions, or for the on-line encapsulation of biologic objects, such as bacteria and cells [5-7]. The topic has been abundantly reported in the Literature [8], and some applications are now commercialized [9]. In such devices, a microflow is dispersed into droplets at the contact of an immiscible secondary flow. This microflow is called the dispersed phase because it is later dispersed in droplets, and the secondary flow, the continuous phase that will transport the droplets. The principle is to use “controlled instabilities”. This term might seem to be an oxymoron, but the paradox can be easily be explained: on one hand, the instabilities are pertaining to the Plateau-Rayleigh type of instabilities that break a microfluidic jet into droplets; on the other hand, geometrical constraints are used to control the jet breakup. Figure 1 shows the controlled breakup of an aqueous alginate microflow in a mFFD.

For encapsulation applications, the particles, or cells, etc., are transported by the dispersed phase. When droplets form, they are engulfed or encapsulated in the droplets. Live cells, bacteria, spores have been encapsulated in such devices. More recently investigations have been performed to make the concept more versatile. An example is furnished in Figure 2 where “multi-branched” FFD has been developed to perform specific tasks. By instance the device of Figure 2.b can be used to add gelling agent to the incoming oil phase for the gelation of the shell [10] while Figure 2.c is a double-FFD used for a double-layer encapsulation [11-14].

From the encapsulation standpoint, there is a definite need for controlling the contents encapsulated in a droplet. It has been observed that many capsules are produced empty, with no content in them, just because the transported particles are randomly dispersed in the incoming microflow.
All the empty capsules must be discarded later by a sorting process. It is a time consuming process, not compatible with an integrated system. Hence, researchers have started investigations on this problem; they have focused on the ordering of the transported objects upstream of the device. For example, Edd and colleagues have searched the geometrical conditions in the injection channel to order the particles [15]. On the other hand, because encapsulation is often performed in polymeric solutions, such as alginates or other polysaccharides, Nam and colleagues, and D’Avino and colleagues have searched the conditions for alignment in a viscoelastic microflow [16, 17]. But these solutions are difficult to integrate in a microdevice, because they require a very long upstream channel to achieve ordering of the particles, they also require very precise flow rate conditions.

In this work, we have designed a new passive concept where a droplet is formed only if there is content present, suppressing the formation of empty droplets. It is based on the possibility of the incoming dispersed phase to escape upstream from the junction (orifice), hence the name EFFD, for “escape FFD”. It is a passive system, not requiring additional energy source, such as electrical power or acoustic source.

We first present the concept of the system, then we derive the pressure conditions for a proper functioning of the device, and finally we present an experimental realization.

II. THE CONCEPT OF EFFD

The principle is to authorize the dispersed phase—the phase which is later dispersed into droplets—to escape in side “moustaches” or “escape paths” just upstream of the orifice, as shown in Figure 3. These moustaches have a small orifice and are placed as close as possible from the orifice. In absence of particles transported by the dispersed phase—i.e. the dispersed phase is a homogeneous liquid—a meniscus remains stable at the orifice at least when the pressure (or flow rate) conditions are adequately chosen. No drop is then produced. Note that the stability of the meniscus requires very stable hydrodynamic conditions, and very-stable, pressure-actuated micropumps are a preferred solution.

A sufficiently large incoming particle cannot escape through the moustaches because their orifice is small. It is trapped in the vicinity of the meniscus. In our original concept [18], it was expected that a large particle—of diameter comparable to the inner dimensions of the channel—trapped at the interface, will restrict the section available for the escape flow at the moustache orifice; the pressure at the meniscus then increases, until the meniscus breaks and a droplet containing the particle is released. After our experimental investigations, the phenomena appeared to be more complex because the system also works for smaller particles. Probably—this is what we infer from the experimental results—the dynamic pressure on the droplet contributes to the deformation of the stable interface, making it bulge and leading to its breakup.

Fig. 3 Sketch of the functioning of the device: (a) in absence of transported object, a meniscus remains stable at the orifice; (b) an incoming large particle is trapped in the vicinity of the interface; (c) an overpressure builds up and the interface breaks; (d) a droplet containing the particle is released and the meniscus pins again at the orifice

The concept has even been extended to a device using a few pairs of moustaches (Fig. 4). In this conceptual design, it is expected that two or more spherical particles will be expelled together, as will be discussed in Section V.

Fig. 4 Sketch of an EFFD: (a) with one pair of moustaches; (b) with two pairs of moustaches

The principle is based on the possibility to obtain a stable meniscus. Experimentally it is very difficult to determine the adequate inlet pressures range. Thus, a theoretical approach has been developed. In the following section, we derive the hydrodynamic conditions for obtaining a stable interface in absence of any incoming particle.

III. MENISCUS STABILITY

In this section we investigate the hydrodynamic conditions before the arrival of a particle, for which a stable meniscus is observed. In this approach, Newtonian fluids are considered. The calculation, however, can be done in a similar, but more complicated approach for non-Newtonian visco-elastic fluids which are often used as the dispersed phase. The derivation of the hydrodynamic conditions for non-Newtonian fluids can be found in Appendix A, and we consider here Newtonian fluids.

An interface pinned at its two ends is stable when the pressure difference across the meniscus does not exceed the Laplace pressure [19]. Let us first calculate the pressure in each channel. In the laminar approach, the general formula
for the pressure drop of a Newtonian fluid, in a channel of hydraulic resistance $R$ is [20, 21]

$$\Delta P = RQ.$$  \hspace{1cm} (1)

The value of $R$ for rectangular channel is presented in Appendix B. Hence, the total pressure drop in a complete channel, from inlet to outlet, is

$$P_{in} = \sum_j R_j Q_j$$  \hspace{1cm} (2)

where the index $j$ denotes all the different sections of the network affected by the flow rate $Q_j$, and $P_{in}$ is the inlet pressure. The outlet pressure is the atmospheric pressure and has been set to zero for simplicity.

Consider first the continuous phase circuit (index $e$), where the upstream flow rates are $Q_e$. The pressure at the interface in the oil phase is then

$$P_{men,e} = 2\sum R_{downstream,e} Q_e$$  \hspace{1cm} (3)

where $P_{men,e}$ is the pressure at the meniscus in the oil phase, and the coefficient 2 corresponds to the double flow rate $Q_e$ downstream from the meniscus. On the other hand, the total pressure drop in the oil phase is

$$P_{in,e} = \sum R_{upstream,e} Q_e + 2\sum R_{downstream,e} Q_e$$

$$= \sum\left(R_{upstream,e} + 2 R_{downstream,e}\right) Q_e$$  \hspace{1cm} (4)

Combination of (3) and (4) yields

$$\frac{P_{men,e}}{P_{in,e}} = \frac{2\sum R_{downstream,e}}{\sum\left(R_{upstream,e} + 2 R_{downstream,e}\right)}.$$  \hspace{1cm} (5)

Using the same arguments for the dispersed phase, it can easily be shown that

$$\frac{P_{men,i}}{P_{in,i}} = \frac{1}{2}\sum R_{downstream,i}$$  \hspace{1cm} (6)

where the coefficient $1/2$ stems from the fact that there are two symmetrical moustaches, so that the flow rate $Q_i$ is divided in two at the moustaches’ orifice.

Finally, using (5) and (6),

$$\frac{P_{men,i} - P_{men,e}}{P_{in,i}} = \frac{1}{2}\sum R_{downstream,i}$$  \hspace{1cm} (7)

Using Laplace theorem, this pressure difference must not exceed

$$P_{men,i} - P_{men,e} = \frac{\gamma}{R_k} + \frac{\gamma}{R_v}.$$  \hspace{1cm} (8)

where $R_k$ and $R_v$ are the horizontal and vertical minimum curvature radii of the meniscus, and $\gamma$ the water-oil surface tension. Using the approximations $R_k \approx w/2$ and $R_v \approx d/2$, where $w$ and $d$ are respectively the width and depth of the channel [15], relation (8) becomes

$$P_{men,i} - P_{men,e} \approx \gamma \left(\frac{1}{w} + \frac{1}{d}\right).$$  \hspace{1cm} (9)

Let us assume for simplicity that the orifices of the moustaches are perfect (ideal case) and that the contact angle is 90°. The meniscus is stable if

$$0 \leq P_{men,i} - P_{men,e} \leq 2\gamma \left(\frac{1}{w} + \frac{1}{d}\right).$$  \hspace{1cm} (10)

In reality, in order to obtain aqueous droplets in an organic phase, the channels are siliconized, and the contact angle is closer to 100-105° (Fig. 5). In this case, relation (10) must be corrected by

$$2\gamma \sin\left(\theta - \frac{\pi}{2}\right)\left(\frac{1}{w} + \frac{1}{d}\right) < P_{men,i} - P_{men,e} < 2\gamma \left(\frac{1}{w} + \frac{1}{d}\right).$$  \hspace{1cm} (11)

Note that (11) collapses to (10) for $\theta = 90\degree$. Let us note

$$\alpha = \frac{1}{2}\sum R_{downstream,i}$$  \hspace{1cm} (12)

and

$$\beta = \sum R_{upstream,e} + 2 R_{downstream,e}.$$  \hspace{1cm} (13)

Then, combining (7) and (11) yields the conditions

$$\frac{2\gamma \sin\left(\theta - \frac{\pi}{2}\right)}{\alpha}\left(\frac{1}{w} + \frac{1}{d}\right) + \frac{\beta}{\alpha} \frac{P_{in,i}}{P_{in,e}} < 2\gamma \left(\frac{1}{w} + \frac{1}{d}\right).$$  \hspace{1cm} (14)

This condition has been graphically represented in Figure 6. The meniscus stability region is the diagonal band in the figure. For the dimensions $w=d=150$ µm, and $\gamma \approx 40$ mN/m, and an approximate value $\theta \approx 0.8$, the width of the stability band is approximately $\frac{2\gamma}{\alpha}\left(\frac{1}{w} + \frac{1}{d}\right)\approx 1500$ Pa. Note that the width of the stability band depends only on $\theta$, not on $\gamma$. This sensitivity is obtainable using high precision micropumps (for example Fluigent®).
Fig. 5 Sketch of the two limit locations of the pinned interface for a two-dimensional case: (left) for a contact angle of 90°, the lower limit is a flat interface and the upper limit a ½ circle; (right) for a contact angle of 105°, the upper limit is still a ½ circle, but the lower limit is slightly bulging.

Below the lower limit the meniscus recedes inside the channel.

IV. EXPERIMENTAL RESULTS

Due to the strict constraints on the geometry, the device has been fabricated in silicon. Conventional DRIE etching has been used, and a glass cover is sealed on top of the system. The dimensions of our first system are shown in Figure 7. The moustache orifice being 30 µm, and the width and depth of the channels being \( w = d = 150 \mu m \), it is expected that the system will work for particles between 30 and 150 µm.

Figure 8 shows the trapping of a hollow glass sphere followed by its expulsion inside a droplet. The dispersed phase is water and the continuous phase is mineral oil.

The sketch of a particle trapped at the interface is shown in Figure 9. The particle and the droplet have been underlined, but the original movie can be found in the ESI.
V. DISCUSSION AND CONCLUSION

The detailed physical mechanisms leading to the droplet formation is not yet fully understood. We are expecting that the particles gathering at the interface would contribute to increase the pressure at the interface by clogging the moustaches. The principle is shown in Figure 10 where the results of a finite element model (COMSOL [22]) show the increase of velocity at the moustache orifice and an increase of the pressure on the sphere. In the calculation, the interface is supposed rigid, in order to avoid the complex problem of a two-phase flow with a moving spherical object. The pressure increases considerably upstream from the sphere and a downwards force is exerted on the sphere. If this force is larger than that of Condition (11), the interface breaks and a droplet containing the sphere is expelled.

Similar calculation can be done for two or more spherical particles showing a larger increase of the pressure with the number of trapped particles (Fig.11). It can also be performed in the case of two pairs of moustaches.

On the other hand, the experiments have shown that the device works with smaller particles which clog much less the moustaches. In such a case, we believe that it is the dynamic pressure on the particles that drives the expulsion of the particle with the droplet, combined to a capillary effect [3]. This is what appears in the movies from the ESI.

Encapsulation is a vast domain. It encompasses biologic applications as well as material sciences applications. In the first case, the objects to encapsulate are most of the time deformable, aqueous-based objects, such as cells and bacteria. In the second case, the capsule content is often rigid, such as solid beads or shells. So far our experiments have used only rigid polystyrene or glass spheres. It is not yet known how deformable biologic objects will behave in the system. This is an important point that needs to be further investigated.

In the future, it would also be of interest to investigate whether multi-FFD systems, such as the one sketched in Figure 2.c, can be implemented with EFFDs in series. At a first sight, it seems possible to obtain stable interfaces when no particle circulates in the system. However, the remaining question is whether a droplet released at the first EFFD will trigger instantaneous interface instability in the second EFFD, leading to the emission of an empty droplet.

In conclusion, in this work, a novel flow-focusing device (EFFD), using escape channels or moustaches at the dispersed phase flow orifice, has been presented. It automatically suppresses the formation of droplets without particulate content. Droplets form only at the arrival of one or more particles. More study is needed to determine the best conditions for the encapsulation of one particle at the time, and to investigate the behavior of deformable objects.

REFERENCES

APPENDIX A: NON-NEWTONIAN APPROACH

In the (frequent) case of a «power-law» or Waele-Ostwald fluid [23], the fluid viscosity can be expressed by

\[ \eta = \frac{\tau}{\dot{\gamma}} = K \dot{\gamma}^{n-1} \quad (15) \]

where \( K \) and \( n \) are coefficients depending on the concentration in polymers, and \( \dot{\gamma} \) the shear rate. For example, in the case of a 1.25 wt% Keltone alginate concentration, \( K=0.5 \) and \( n=0.8 \). For cylindrical channels Rabinowitsch and Mooney have derived a closed form expression for the pressure drop [24,25]

\[ \Delta P = \frac{2KL}{r^{n+1}} \left( \frac{3n+1}{n} \right)^n \left( \frac{3n+1}{n} \right)^n \frac{Q^n}{Q^n} \quad (16) \]

where \( L \) is the length of the cylinder and \( r \) its radius. We can define a hydraulic resistance by

\[ R = \frac{\Delta P}{Q} = \frac{2KL}{r^{n+1}} \left( \frac{3n+1}{n} \right)^n \frac{Q^n}{Q^n} \quad (17) \]

To the difference with the Newtonian case, the hydraulic resistance depends on the flow rate. For rectangular channels, the pressure drop can be approximated by [26-28]

\[ \Delta P = \frac{KL}{D_h} \left( \frac{1}{w d} \right)^{2n+2} \left( \frac{c_1}{n} + \frac{c_2}{n} \right) \left( \frac{2(1+\varepsilon)}{\sqrt{\varepsilon}} \right) \frac{Q^n}{Q^n} \quad (18) \]

where \( D \) is the hydraulic diameter \( D = 2wd \) and \( \mathcal{C} \) the aspect ratio \( \varepsilon = \min \left( \frac{w}{d}, \frac{d}{w} \right) \). The constants \( c_1 \) and \( c_2 \) are given by

\[ c_1 = \frac{3}{2} \left( 1 + \varepsilon \right) \left( 1 - \frac{32}{\pi^3 \cosh \left( \frac{\pi}{2 \varepsilon} \right)} \right) \quad (19) \]

\[ c_2 = 1 - \frac{192}{\pi^5 \tanh \left( \frac{\pi}{2 \varepsilon} \right)} \quad (19) \]

The hydraulic resistance is then

\[ R = \frac{\Delta P}{Q} = \frac{KL}{D} \left( \frac{1}{w d} \right)^{2n+2} \left( \frac{c_1}{n} + \frac{c_2}{n} \right) \left( \frac{2(1+\varepsilon)}{\sqrt{\varepsilon}} \right) \frac{Q^n}{Q^n} \quad (20) \]

We can then write

\[ P_n = \sum_j R_j Q = K \sum_j R_j^* Q^n \quad (21) \]

where

\[ R_j^* = f \left( D_j, w_j, d_j, L_j, n \right) = \frac{L_j}{D_j} \left( \frac{w_j d_j}{2} \right)^{3n+1} \left( \frac{c_{1,j}}{n} + \frac{c_{2,j}}{n} \right) \left( \frac{2(1+\varepsilon)}{\sqrt{\varepsilon}} \right) \]

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\[ \eta = \frac{\tau}{\dot{\gamma}} = K \dot{\gamma}^{n-1} \quad (15) \]
The coefficient $R_j^*$ depends on the geometry and on the exponent $n$. The pressure at the meniscus is then given by

$$\frac{P_{\text{men}}}{P_{\text{in}}} = \frac{KQ^n \sum_{j \in \text{downstream}} R_j^*}{KQ^n \sum_{j \in \text{all}} R_j^*} = \frac{\sum R_j^*}{\sum R_j^*}$$

(22)

This expression is very similar to that found for Newtonian fluids (6); the difference stems from the expressions of the hydraulic resistances. Note that only one of the two coefficients of the viscoelastic rheology appears in (22): the exponent $n$ is present in (22) while $K$ is absent.

APPENDIX B: HYDRAULIC RESISTANCE OF NEWTONIAN FLUIDS IN RECTANGULAR MICROCHANNELS

There exist a few expressions for the hydraulic resistance of a square microchannel [20,21]. We have tested with success the one from Barhami and colleagues [29]

$$R = \frac{8\eta L}{wd \min(d, w)^2 \chi},$$

(23)

where $w$, $d$ and $L$ are respectively the width, depth and length of the channel, $\eta$ the dynamic viscosity, and $\chi$ an aspect ratio factor. This function can be expressed by

$$\chi = 2 \left( \frac{1}{3} - \frac{64 \varepsilon}{\pi^5} \tanh \frac{\pi}{2 \varepsilon} \right),$$

(24)

where $\varepsilon$ is the aspect ratio: $\varepsilon = \min(w/d, d/w)$. 

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